Evolution of Rising Magnetic Cavities and UHECR acceleration

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Structure of Clusters and Groups of Galaxies in the Chandra Era, Boston, July 12-14 2011

#### Outline

- Solutions for static cavities
- Self similarly and quasi statically expanding cavities
- Formation of reconnection layer and cosmic ray acceleration

X-ray cavities

 Areas of lower X-ray emission in galaxy clusters (Fabian et al. 2001, Churazov et al. 2001, Birzan et al. 2004, Diehl et al. 2008)

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- Lower density and higher temperature
- They are related to AGN activity



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Hydra A cluster, z=0.054,T=10<sup>7</sup>K, size ~ 200kpc, Image: NASA/CXC/U.Waterloo/C.Kirkpatrick et al. 2009

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- We start from static solutions of the Grad-Shafranov equation (Shafranov 1966)

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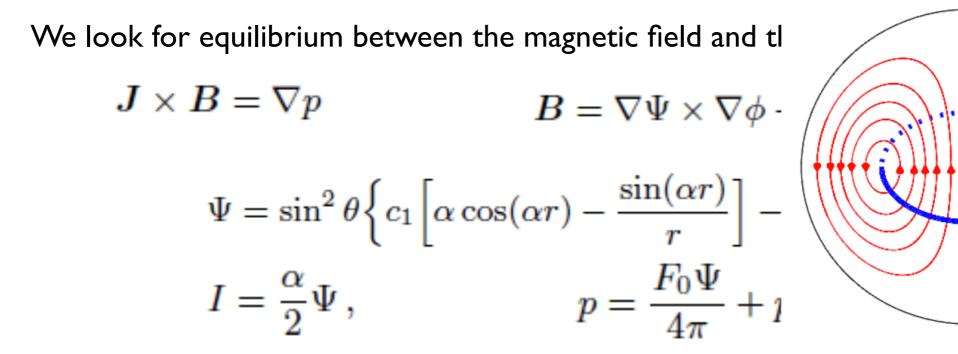
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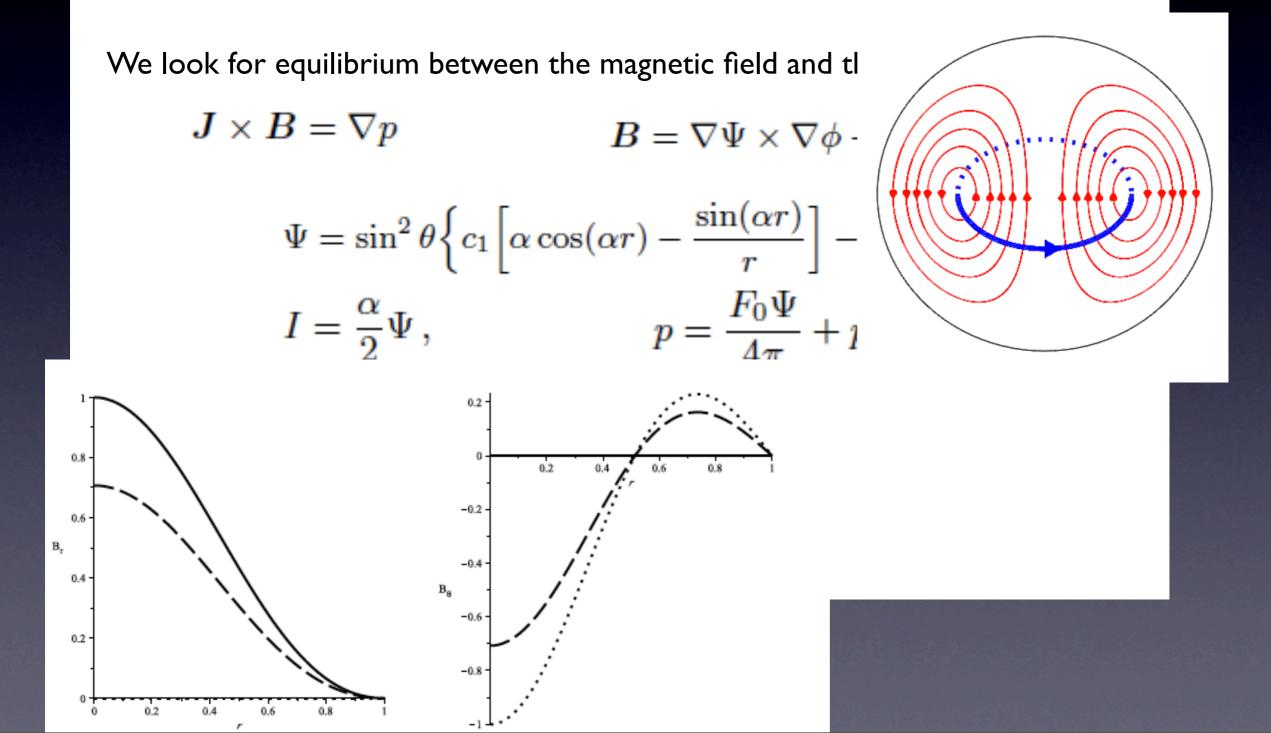
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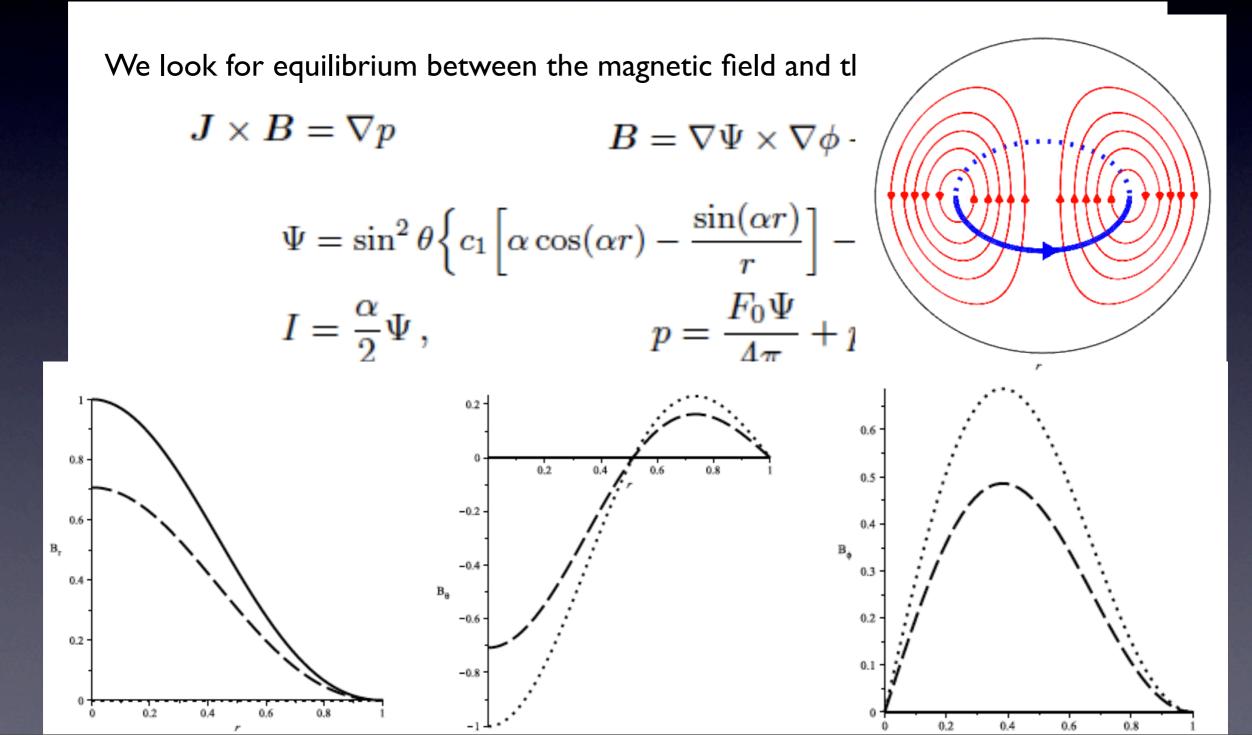
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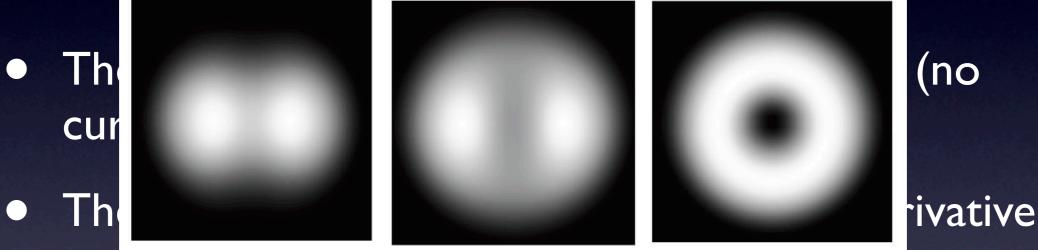
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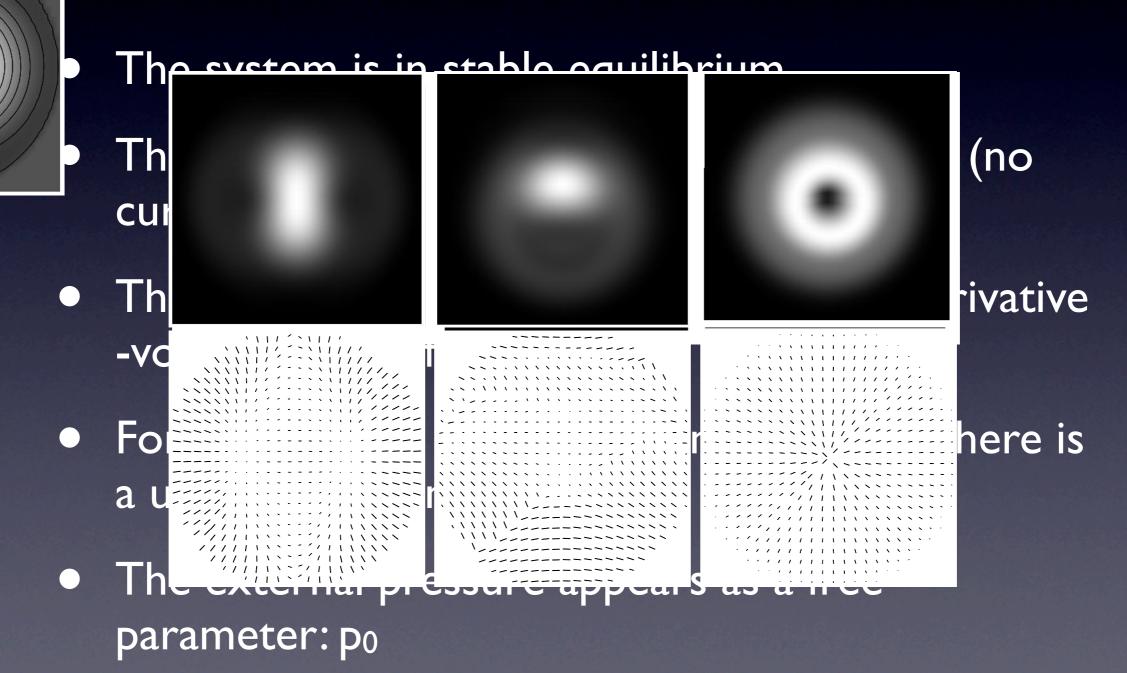
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#### MHD simulations

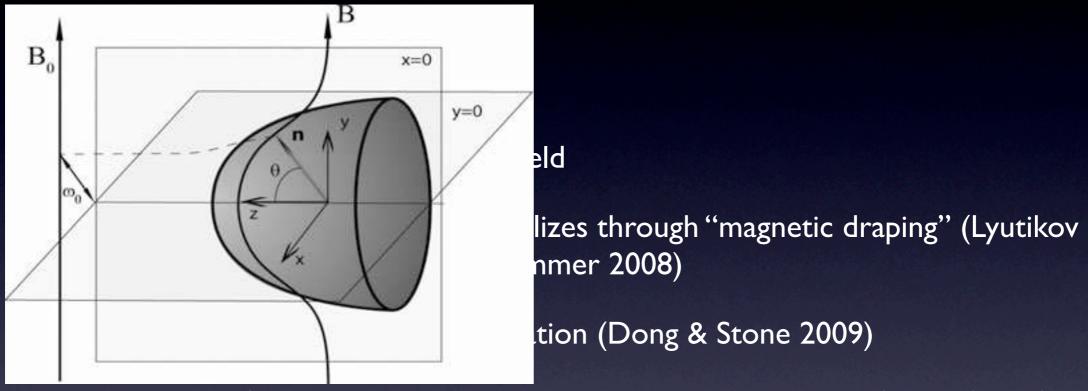
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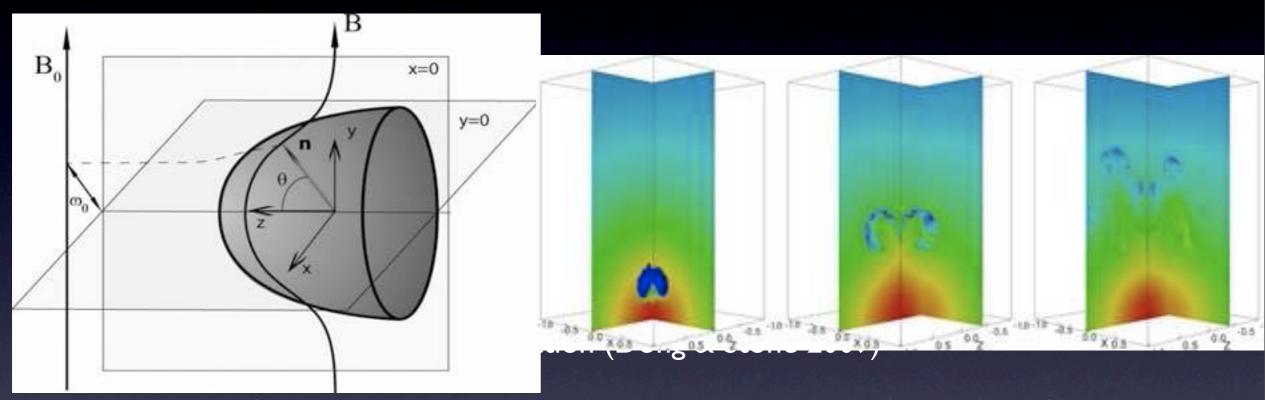
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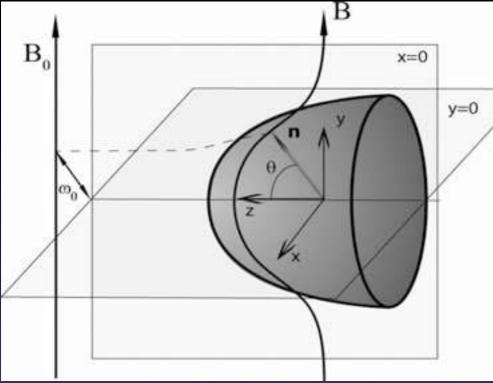
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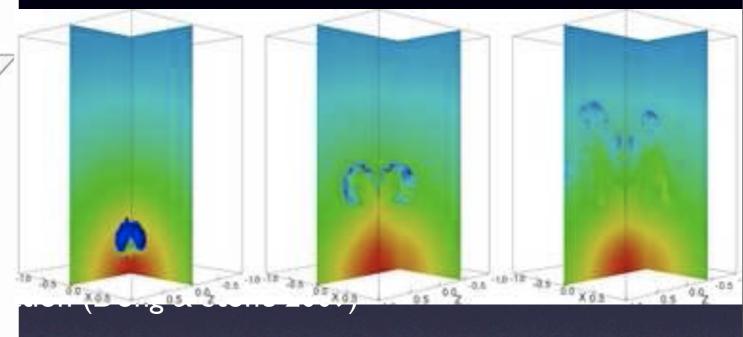


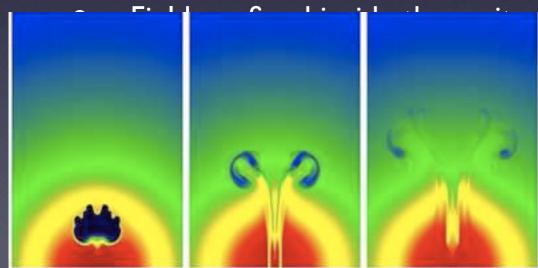
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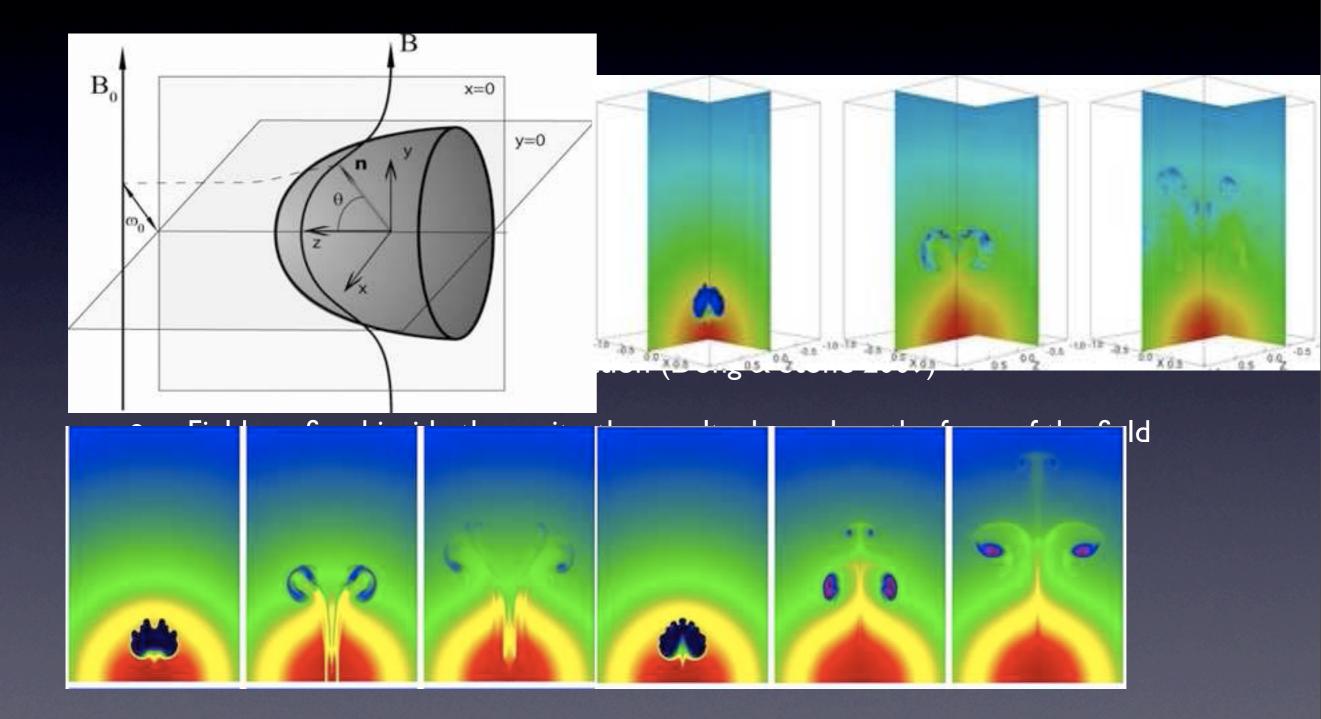
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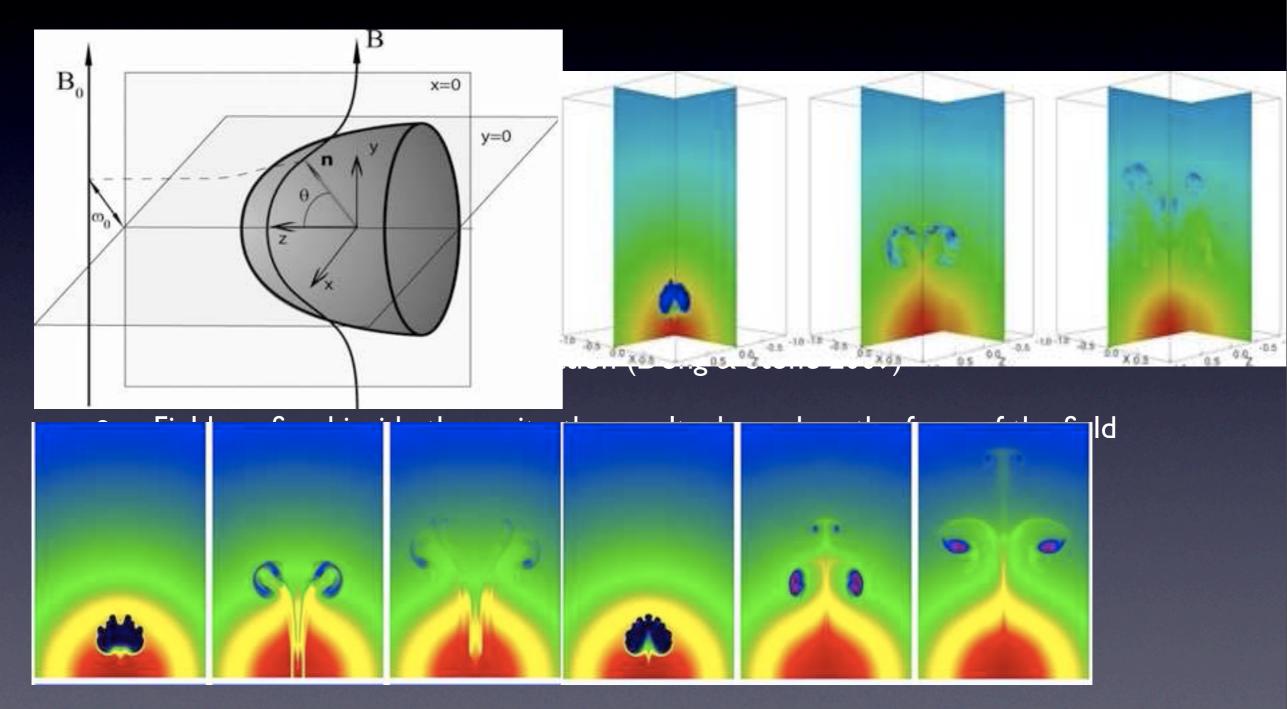






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Figures: Lyutikov 2006, Dong & Stone 2009

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In the quasi-static formulation we require:

- conservation of magnetic flux, helicity and mass
- force equilibrium (RHS of momentum equation)
- $\Gamma$  is not constrained to 4/3

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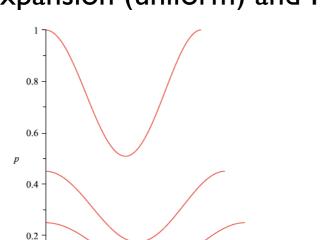
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0.4

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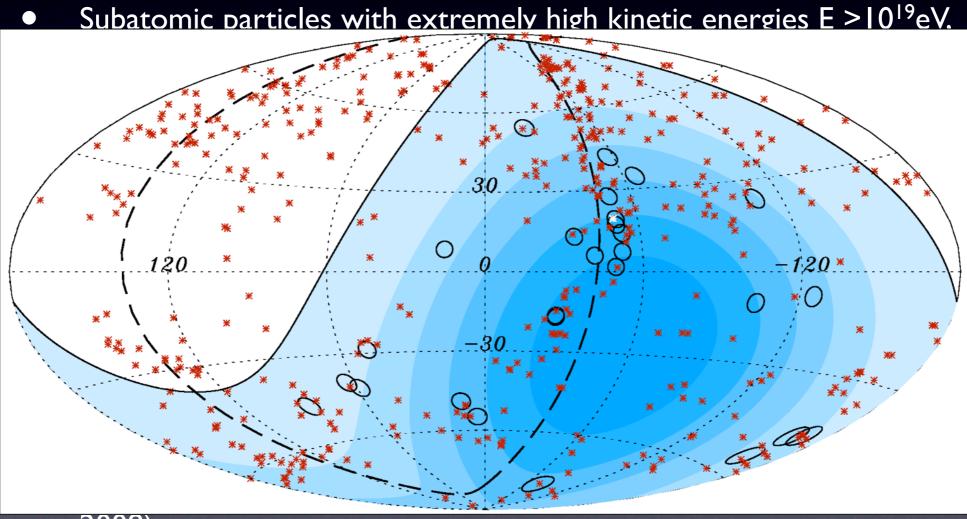
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- Acceleration sites: jets-shocks (AGN and GRBs, i.e. Lazarian & Vishniak 1999, Giannios 2011), Fossil lobes (Benford & Protheroe 2008)



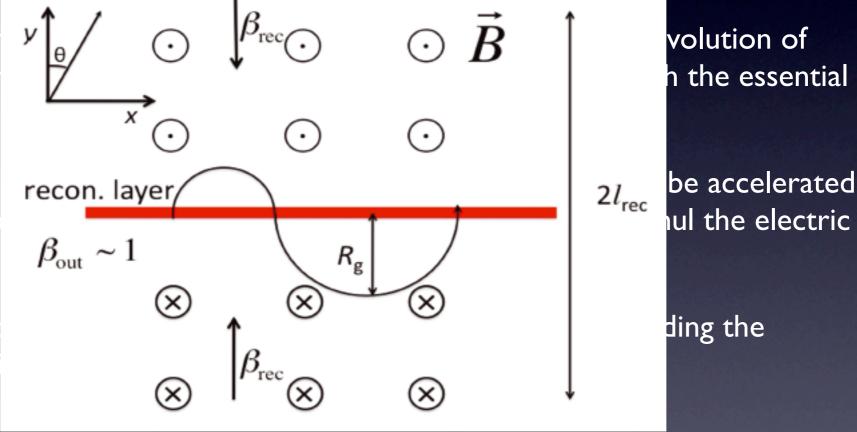
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- They provide the essential potential for UHECR acceleration if we consider one of the known mechanisms
- When reconnection layers form we break the initial assumption of ideal-MHD, formally we cannot predict the next step of evolution, but we do not expect destruction of the cavity