SHERPA

The Modeling and Fitting Application of the CIAO Software System

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Flexible Analysis in Sherpa

(There is no single, correct path to every final answer.)

- To analyze high-resolution spatial, spectral, and temporal data, one must overcome a slew of obstacles: for instance, fitting techniques based on the Gaussian distribution may not apply when the number of counts in each bin is low, or determining the best-fit of a complex model may not be easy.
- Sherpa thus provides many fit statistics and methods of optimization and parameter estimation that have different underlying assumptions and/or provide different strategies for dealing with difficult analysis problems.
- The cutting-edge nature of these analysis obstacles has led to an astrostatistics collaboration between the *Sherpa* team and members of Harvard University's Department of Statistics.

Selected Sherpa References

- As used to fit *Chandra* spectra of quasars, jets, and clusters:
 - Cappi et al., ApJ, 2001
 - Marshall et al., ApJL, 2001
- As used to fit *Chandra* images:
 - Cagnoni et al., in preparation, 2001
- As used to fit *ROSAT* images:
 - Paolillo et al., in preparation, 2001
- As used to fit multi-wavelength data:
 - The Large Bright Quasar Survey (Forster et al., ApJS, 20 Nov 2000)
 - The H/RCULES Project (Forster et al., AAS, 2000)

A Typical Sherpa Session

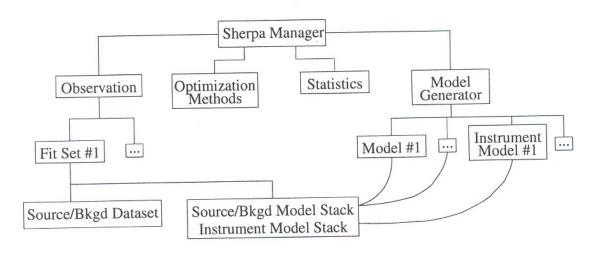
(The boiled-down version.)

The user:

- reads in data (and sets filters, etc.);
- builds model expressions;
- chooses a statistic;
- fits the model expressions to the data, one at a time;
- compares the results of the fits in order to select a best-fit model; and
- estimates the errors for the best-fit model parameters.

Sherpa: Under the Hood

• Sherpa is an object-oriented C++ application:



Simplified Relationship Diagram
(Not a Class Diagram!)

• A global pointer in **Sherpa Manager** allows communication between "widely separated" *Sherpa* objects.

Data Entry

- During a *Sherpa* session, the user may read in files containing:
 - source data
 - background data
 - errors on the source and/or background data
 - filters
 - statistical weights

These data may be integer, float, or double precision and may be of arbitrary dimensionality.

- Currently supported file types include:
 - ASCII
 - FITS binary table
 - FITS image
 - PHA types I & II
 - IRAF imh
 - ROSAT qpoe

For all types except ASCII, data entry is accomplished through the Data Model interface, so that, *e.g.*, one can use the Data Model filtering syntax within *Sherpa* data entry commands.

- In *Sherpa*, one can build model expressions that represent the
 - source
 - background
 - instrument

for each dataset.

- \Rightarrow Note, however, background and instrument model expressions are *not* required to carry out fits.
- Currently, nearly 40 one- and two-dimensional *Sherpa* models and 90 one-dimensional *XSPEC v. 11* models are available for building model expressions.

• The *Sherpa model language* resolves ambiguity by allowing the user to give a unique name or alias to each instance of a model.

• Example:

- If two datasets are entered, and each is to be fit with a different Gaussian model:

```
sherpa> gauss1d[g1]
sherpa> gauss1d[g2]
sherpa> source 1 = g1
sherpa> source 2 = g2
```

- If, on the other hand, they are to be fit with the same Gaussian model:

```
sherpa> gauss1d[g1]
sherpa> source 1:2 = g1
```

- Note the similarity to object-oriented programming:
 - gauss1d can be considered the blueprint "class."
 - g1 and g2 can be considered "instantiated objects"
 of "class" gauss1d.

- Model parameters can be *linked* to other parameters.
- Example:
 - A particular atomic line is observed by detectors with different resolutions. One can model this line with two Gaussian functions whose centroids (but not amplitudes or widths) are linked:

```
sherpa> source 1 = gauss1d[g1]
sherpa> source 2 = gauss1d[g2]
sherpa> g1.pos => g2.pos
```

- Model parameters can also be linked to other models.
- Example:
 - One can model emission from an accretion disk using a blackbody function whose temperature is a function of radius:

```
sherpa> Temperature = POLY
sherpa> BB.kT => Temperature
```

• A model can be *nested* within another model.

• Example:

- Transform an input dataspace to log-space, and evaluate a blackbody in that space:

```
sherpa> logenergy = shlog
sherpa> source = bb{logenergy}
```

• Different models can be defined along each axis of a multi-dimensional dataset.

• Example:

Model two-dimensional data that have spectral information along one axis and spatial information (e.g. radius) along the other:

```
sherpa> data image.fits
sherpa> lorentz[Spatial]
sherpa> pow[Spec]
sherpa> source = Spatial{x1}*Spec{x2}
```

Instrument Models

- Instrument models describe the mapping from photon space (where source and background models are evaluated) to counts space (where fit statistics are computed) for a particular detector.
 - ⇒ The instrument model class, by hiding detectordependent details, allows Sherpa to be a missionindependent fitting application.
- Currently *Sherpa* offers three instrument model types:
 - RSP, in which the evaluated one-dimensional model is multiplied by an ancillary response (i.e. effective area) and then folded through a response matrix;
 - PSFFromTCD, in which the evaluated one- or two-dimensional model is convolved with an analytic kernel (e.g. Gaussian) defined in CIAO's TCD library;
 - and PSFFromFile, in which the evaluated two-dimensional model is convolved with a numeric kernel.

Optimization in Sherpa

Optimization is the action of minimizing χ^2 or $-\log \mathcal{L}$ by varying the thawed parameters of the model. The user may choose between several optimization methods in Sherpa, including ones which:

- Find the local minimum.
 - POWELL
 - SIMPLEX
 - LEVENBERG-MARQUARDT

These algorithms are not computationally expensive, but they are also not appropriate for finding the global minimum of a complex statistical surface when starting from a random point.

- Attempt to find the global minimum.
 - GRID and GRID-POWELL
 - MONTE and MONTE-POWELL
 - SIMULATED ANNEALING

These are computationally intensive algorithms which are useful for searching complex statistical surfaces, starting from a random point.

Parameter Estimation in Sherpa

Currently available parameter estimation methods:

- UNCERTAINTY
- PROJECTION (or the profile likelihood)
- COVARIANCE

Parameter estimation methods that will eventually become available to *Sherpa* users:

- Data simulation and fitting
- The Laplace Approximation
- Numerical integration via brute force
- Numerical integration via BAYESPACK
- Markov-Chain Monte Carlo

χ^2 -Based Statistics

The χ^2 statistic is

$$\chi^2 \equiv \sum_i \frac{(D_i - M_i)^2}{\sigma_i^2} \,,$$

where

- D_i represents the observed datum in bin i;
- M_i represents the predicted model counts in bin i; and
- σ_i^2 represents the variance of the sampling distribution for D_i .

χ^2 Statistic	σ_i^2
GEHRELS	$[1+\sqrt{D_i+0.75}]^2$
DVAR	D_i
MVAR	M_i
PARENT	$\frac{\sum_{i=1}^{N} D_i}{N}$
PRIMINI	M_i from previous best-fit

Likelihood-Based Statistics

The CASH statistic is

$$C \equiv 2\sum_{i}[M_{i}-D_{i}\log M_{i}] \propto -2\log \mathcal{L},$$

where

- D_i represents the observed datum in bin i;
- M_i represents the predicted model counts in bin i; and
- $\mathcal{L} = \prod_i \frac{M_i^{D_i}}{D_i!} \exp(-M_i).$

```
Sherpa: Modeling 2D image data, X-ray cluster
paramprompt off
data image small.fits
image data
# load the region file to ds9
# Region: Load src3.reg
ignore image
# inspect the filter
image filter
image data
source = beta2d[b2]
# b2.r0 parameter value [350]
# b2.alpha parameter value [1]
# b2.xpos parameter value [217.5]
# b2.ypos parameter value [204.5]
# b2.ellip parameter value [0]
# b2.theta parameter value [0]
# b2.ampl parameter value [12]
# freeze b2.xpos
# freeze b2.ypos
statistics cash
# fit
# CTRL-C
#sherpa> fit
# LVMQT: V2.0
# LVMQT: initial function at value = 7.33261e+06
# LVMQT: iteration limit reached
# LVMQT: final function value = 120186 at iteration 100
#
            b2.r0 32.663
#
            b2.alpha 1.23249
            b2.ampl 2.61009
# Include ellipticity and theta
thaw b2.ellip
thaw b2.theta
fit
```

```
# ctrl-C
# read saved parameter values

use session.1
image fit
# tile frames, show data, model, errors in three frames
# create new frame and display residuals there
# image residuals
# write res.fits
# run csmooth - adaptive smoothing with Gaussian kernel
# and look at the results
# # load res_smth4.fits to ds9, zoom
```

```
# Example of Sherpa session in CIAO 2.0 for image analysis
# using a PSffromFile as a model
data center img.fits
# to display
image data
# to see current setup
show
parampromt off
source = psffromfile[mypsf]
show mypsf
#PSFfromFile[mypsf]
    Param Type Value Min
                                                  Max
                                                                            Units
# 1numCuts frozen 1 1 1 # 2convTyp frozen 1 1
                                                       2
# 3 file string: "good.psf.float.fits "
# 4 xsize frozen 32 1
# 5 ysize frozen 32 1
# 6 xoff frozen 0 -512
# 7 yoff frozen 0 -512
# 8 xpos thawed 512 1
# 9 ypos thawed 512 1
# 10 norm frozen 1 0
                                                 1024
1024
                                                51<sub>2</sub>
1024
1024
                                                    1000
# Parameters of PSFfromFile are listed above and you can set
# parameters for fitting. Also you can display
# your psf
image psf
statistics Cash
thaw mypsf.norm
fit
# image fit creates images in 3 frames
image fit
write residuals
```